

Geometry: Please clear your desk except for ...

1. Assignment #13

2. Determine the truth of the following statement and it's converse.

If $2x-3=7$, then x is greater than 0.

Can you write a true biconditional statement from this information? Explain why you can or cannot.



OS: If $2x-3=7$, then x is greater than 0.

$$\begin{array}{l} H \\ 2x=10 \\ x=5 \end{array} \qquad \begin{array}{l} C \\ 5 > 0 \end{array} \quad \boxed{\text{True}}$$

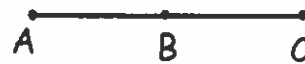
CS: If $x > 0$, then $2x-3=7$.

$$\boxed{\text{False}} \quad \begin{array}{l} CE: x=2 \\ 2 > 0 \end{array} \quad \begin{array}{l} \text{Hyp true} \\ \text{but } 2(2)-3 \neq 7 \\ 1 \neq 7 \\ \text{Conc. False} \end{array}$$

Can you write a true biconditional statement from this information? Explain why you can or cannot.

You cannot write one because both the OS and CS must be true.

Old: The Midpoint Theorem

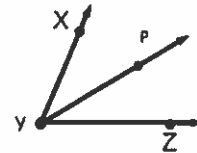


If B is the midpoint of \overline{AC} then

$$AB = \frac{1}{2}AC, \quad BC = \frac{1}{2}AC, \quad \text{and} \quad AB = BC.$$

New: Angle Bisector Theorem (#1)

If \overline{YP} is the bisector of $\angle XYZ$, then

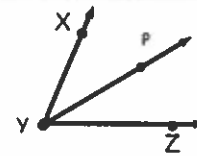


$$m\angle XYP = m\angle PYZ, \quad m\angle XYP = \frac{1}{2}m\angle XYZ, \quad m\angle PYZ = \frac{1}{2}m\angle XYZ \quad \odot$$

Angle Bisector Theorem (#1)

Given: \overline{YP} is the bisector of $\angle XYZ$

Prove: $m\angle XYP = m\angle PYZ, m\angle XYP = \frac{1}{2}m\angle XYZ, m\angle PYZ = \frac{1}{2}m\angle XYZ$



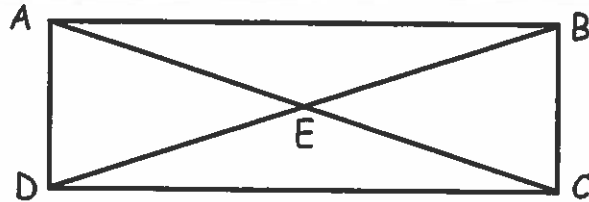
Statements	Reasons
1. \overline{YP} is the bisector of $\angle XYZ$	Given
2. $\angle XYP \cong \angle PYZ$	Def. of \angle Bisector
3. $m\angle XYP = m\angle PYZ$	Def. of $\cong \angle$ s
4. $m\angle XYP + m\angle PYZ = m\angle XYZ$	\angle Add. Post.
5. $m\angle XYP + m\angle XYP = m\angle XYZ$	Subst. Prop of = (3 \rightarrow 4)
6. $2m\angle XYP = m\angle XYZ$	Dist. Prop.
7. $m\angle XYP = \frac{1}{2}m\angle XYZ$	Div. Prop. of =
8. $m\angle PYZ = \frac{1}{2}m\angle XYZ$	Subst. Prop of = (3 \rightarrow 7)

Sample Proof:

Given: $AE = DE$;

$EC = EB$

Prove: $\overline{AC} \cong \overline{BD}$



	STATEMENTS	REASONS
1	$AE = DE$; $EC = EB$	Given
2	$AE + EC = DE + EB$	Add. Prop. of $(+)$
3	$AC = AE + EC$; $BD = DE + EB$	Seg. Add. Post.
4	$AC = BD$	Trans. Prop. of $=$
5	$\overline{AC} \cong \overline{BD}$	Def. of \cong Segments

Assignment #14

Read and Take Notes on p. 43-45.

Complete p. 45-47 CE #1-9 and WE #1-8, 13-14, 19, 21.